

# Response of a Magnetic Nanoparticle System to a Rotating Magnetic Field

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## The Model and Simulations: Stoner-Wohlfarth Model+Dipolar Interactions

### Energy of the $i^{\text{th}}$ Magnetic Nanoparticle (MNP) (reduced units):

$$E_i = \frac{1}{2} (\vec{k} \cdot \vec{\mu}_i)^2 + \vec{h} \cdot \vec{\mu}_i + \vec{h}_d \cdot \vec{\mu}_i, \quad \text{with } \vec{h}_d = g \sum_{j \neq i}^N [\vec{\mu}_j - 3(\vec{\mu}_j \cdot \vec{r}_{ij}) \vec{r}_{ij}] / r_{ij}^3$$

Anisotropic energy Zeeman energy Dipolar interactions energy

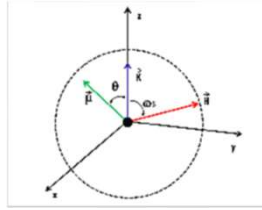
$$\vec{h} = \frac{\vec{H}}{H_A} = \frac{\mu_0 M_S \vec{H}}{2K}, \quad g = \frac{M_S}{H_A}, \quad r_{ij} = \frac{r_{ij}}{D} \quad \text{so } t = \frac{k_B T}{2KV}$$

$\vec{\mu}_i$ : Unit vector of the magnetic moment  $\vec{\mu} = M_S V \vec{\mu}_i$ ;  
 $M_S$ : Saturation magnetization,  $V$ : volume,  $D$ : diameter;  
 $\vec{k}$ : Unit vector of the anisotropy axis  $\vec{K} = K \vec{k}$  assumed uniaxial;  
 $\vec{r}_{ij}$ : Unit vector that joins  $i$  and  $j$  MNPs,  
 $g$ : Dipolar Interaction magnitude

### Rotating External Magnetic Field:

$$\vec{h} = h_0 (0, \cos(\omega s), \sin(\omega s))$$

$\omega$ : angular frequency,  $s$ : MCS time



### MNP Parameters and simulation Details

- Fe MNP monodisperse  $N_p = 100$  spherical particles with diameter  $D = 7.5$  nm,  $K = 4.5 \times 10^4$ ,  $M_S = 1.7 \times 10^6$  A/m;
- Néel relaxation is only allowed;
- The MNP's were randomly distributed in a cubic box of size  $L = 8$  D;
- Direction of  $\vec{k}$ : along z axis, and random;
- Metropolis Dynamics with solid angle restriction [Nowak];
- Thermal reservoir at temperature  $t$ , open boundary conditions;
- The components of the normalized magnetization were measured every  $tm = 120$  MCS

## Results and Discussion:

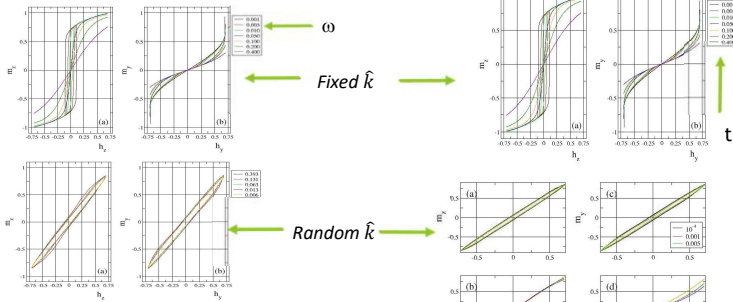
### Non Interacting Model (Stoner-Wohlfarth-SW): $g=0$

[Stoner]

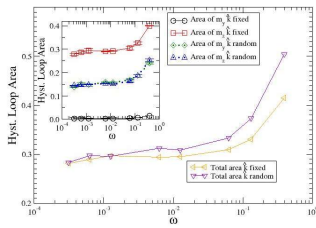
Frequency behavior with  $h_0 = 0.7$  and  $t = 10^{-4}$ :

Hysteresis only in  $m_z$  for fixed  $\vec{k}$  and in both components with  $\vec{k}$  random

Thermal behavior with  $h_0 = 0.7$ ,  $\omega = 0.006$ : vanishing of the blocked state

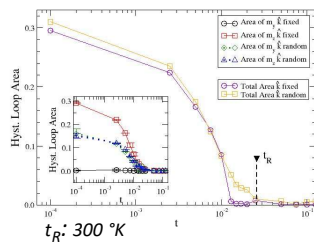


Hysteresis Loop Areas



In both cases, better heat transfers when the MNP's anisotropy axes are directed randomly (no special preparation is required)

Hysteresis Loop Areas



## Conclusions:

### SW model:

- The appearance of hysteresis with temperature in the magnetization components depend on the direction of the anisotropy axes;
- As a function of  $\omega$  or  $t$ , the total area is larger for the random case, and increases the frequency.

### SWD model:

- Hysteresis was observed for all coplanar magnetization components;
- The loop displacement is a consequence of the values of the dipolar field and the phase shift with the external field;
- The peak in the loop areas is associated with an anisotropy increase caused by the dipolar field.
- By comparing the total loop areas, the SW model can transfer an amount of heat than the SWD model at low temperatures, but this behavior is reversed for  $t \geq t_R$

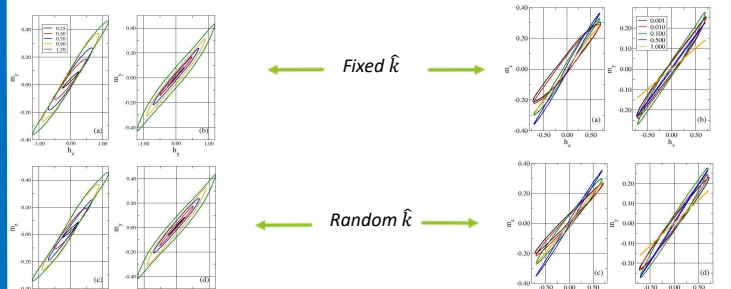
### Interacting Model (Stoner-Wohlfarth+Dipolar interactions-SWD): $g=1.6875$

Low  $t$  Behavior:  $t = 10^{-4}$ ,  $\omega = 0.006$ :

Rounded hysteresis loops that extend beyond the theoretical  $h_0$  interval  $0.5 \leq h_0 \leq 1.0$  [Usov]  
 Displaced loops w/ respect to the origin

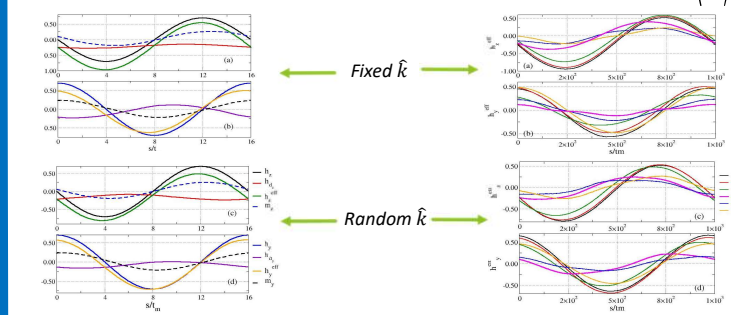
Thermal Behavior:  $h_0 = 0.7$ ,  $\omega = 0.006$ :

Hysteresis in both components beyond  $t_R$  displaced loops that center with  $t$



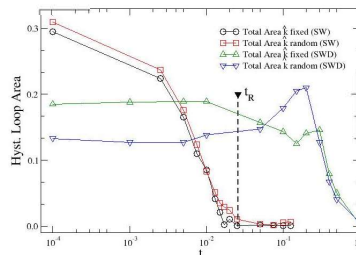
$$\text{Dipolar field per particle: } \langle \vec{h}_d \rangle = 1/N_p \sum_{i=1}^{N_p} \vec{h}_d^i$$

$$\text{Effective field: } \vec{h}^{\text{eff}} = \vec{h} + \langle \vec{h}_d \rangle$$



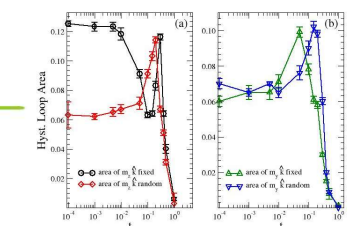
At this temperature, the dipolar field affects the action of the external field causing an effective field that is not symmetrical with respect to the zero-field line since the dipolar field components are negative, and the loops are displaced. So the values of the coercive field in both components are not symmetric. This effect is less relevant in the y components

For  $10^{-2} \leq t \leq 0.5$  the effective fields behave as in the  $t = 10^{-4}$  case causing an effective field that is not symmetrical with respect to the zero-field line since the dipolar field components are negative, and the loops are displaced. For  $t > 0.15$  (not shown)  $h_2^{\text{eff}}(s) = h_2^{\text{eff}}(s \pm p/2)$  where  $p = 1/\omega$ , so the loops become more centered.



References:

- [Stoner] E. C. Stoner and A. Wohlfarth, *Trans. R. Soc. Lond. A* **240**, 826 (1948)  
 [Nowak], U. Nowak, R. W. Chantrell and E. C. Kennedy, *Phys. Rev. Lett* **84**(1):163-6, (2000)  
 [Usov] N. A. Usov, E. M. Gubanov, N. B. Epshtein, G. A. Belayeva, V. A. Oleinikov, *J. Magn. Magn. Mater.* **499**, 166260 (2020)  
 [Saracco] G. P. Saracco and M. A. Bab, *J. Magn. Magn. Mater.* **583**, 171014 (2023)



The peak exhibited in the areas is related to the thermal activation of the dipolar field by temperature and the consequent apparition of the shape anisotropy in the blocked state [Saracco]